## Taking POC for SOC further

## Contents

- Complex systems
- Solving analytically
- Solving numerically
- Catalytic cycles
- Rate-determining steps
- Changes in R.D.S.
- D.F.T. is support of mechanisms
- Correlation with kinetic data


## Episulfonium-ion mediated ring closure



## Episulfonium-ion mediated ring closure



## Integrated rate expressions



$$
\begin{array}{ll}
\frac{d[A]}{d t}=-k^{1}[A]-k^{2}[A] & {[A]=[A]_{0} e^{-(k 1+k 2) t}} \\
\frac{d[B]}{d t}=k^{1}[A]-k^{3}[B] & {[B]=\frac{k_{1}[A]_{0}}{k_{3}-k_{1}-k_{2}}\left(e^{-(k 1+k 2) t}-e^{-k 3 t}\right)} \\
\frac{d[C]}{d t}=k^{2}[A]+k^{3}[B] & {[C]=[A]_{0}\left(1-e^{-(k 1+k 2) t}-\frac{k_{1}}{k_{3}-k_{1}-k_{2}}\left(e^{-(k 1+k 2) t}-e^{-k 3 t}\right)\right)}
\end{array}
$$

## Using MS Excel to solve for the rate constants

| Time | data A data B data C | calc A calc B calc C | error A error B error C |
| :--- | :--- | :--- | :--- |
|  |  |  |  |
| k1 |  |  |  |
| k2 |  |  |  |
| k3 |  |  |  |
| RMS error |  |  |  |

1) Tabulate experimental data
2) Calculate expected values of the time points, for estimated $k^{1}, k^{2}$ and $k^{3}$, using the formulas previously worked out.
3) Calculate error (data - calc) for each point and square it.
4) Calculate average (error${ }^{2}$ ) and square root it. This is the RMS error.
5) Use the SOLVER function in Excel to minimise the RMS error by adjusting $k^{1}, k^{2}$ and $k^{3}$.

## Is it possible to do this without the integration?

YES! Euler's method for solving differential equations numerically.

1) We know the simple rate expressions.
2) Take a guess at the rate constant $k$
3) We know $[A]$ and we know $\frac{d[A]}{d t}$
4) Start at " $t^{1}, A^{11}$ and move a small time step $\delta t$ in direction of gradient
5) $\delta \mathrm{A}=\frac{\mathrm{d}[\mathrm{A}]}{\mathrm{dt}} \delta \mathbf{t}$
6) Calculate $t^{1}+\delta t=t^{2}$ and calculate $A^{1}+\delta A=A^{2}$.
7) Repeat again and again until $t=$ end of reaction
8) Compare the calculated values of $A$ with the experimental values of $A$. Calculate RMS error.

9) Repeat with a new values of rate constant $k$ until error is minimised.

## Is it possible to do this without the integration?

Actually the 4th Order Runge Kutta method is better. And there is plug-in for Excel:
http://www.chem.mtu.edu/~tbco/cm416/RK4_v3_0.html or Google "excel rk4 plug in"

1) Download and install plug-in
2) Get your rate constants and starting concentrations into a .rk4 file (see guide): Sarah.rk4
3) Get your data into .dat file: Sarah8.dat
4) Open Excel and press the RK4 button. Blank.xls

## Using RK4 numerical method



## Catalysis kinetics




## Catalytic cycles



$\frac{\mathrm{d}[\mathrm{prod}]}{\mathrm{dt}}=$ constant
rate determining step must not include free amine starting material

so $A$ is resting state and

$$
\frac{\mathrm{d}[\text { prod }]}{\mathrm{dt}}=\mathrm{k}^{1}[\mathrm{Zr}]
$$

Zero order in SM

## Catalysis kinetics

For a non-catalytic reaction: the reaction rate expression describes the difference in atomic make up between the starting materials and rate determining step

For a catalytic reaction: the reaction rate expression describes the difference in atomic make up between the catalyst resting state and rate determining step


## Changes in Rate-determining step



Noyori, Wills and others

## Reaction mechanism and kinetics



## Reaction mechanism and kinetics



Coupled differential equations: $d[P] / d t$ and $d\left[R u H_{2}\right] / d t$ as functions of $[P],\left[R u H_{2}\right]$ and constants.

## Solving coupled differential equations using MATLAB



## Data from GC and NMR for various catalysts



## Data from GC and NMR for various catalysts



## Changes in RDS due to starting concentrations



## Using modelling to help with TS structure

Kinetics can tell you the atoms in the transition state of the RDS. What about the structure?
Quantum chemical calculations can really help in modelling the structure of the transition state.
e.g.



Adv. Synth. Catal. 2007, 349, 2537 - 2548

## What is in the T.S.?



1st order in
aldehyde


1st order in nitromethane


1st order in catalyst


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## Competing pathways



Starting material complex



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## Modelling the reaction path





Starting complex
G.S.

Reaction T.S.


Product complex G.S.

## Modelling relative rates



Can we use modelling (DFT) to help understand why?

## Getting started in DFT

Commerical software such as Gaussian and Jaguar are widely used (but expensive).
GAMESS and PCGAMESS / Firefly are free!
PCGAMESS is available for windows, mac and linux, and it fast.
Instructions are included and it is simple to set up and use.

Helpful points:
Start on simple systems.
Build up complex systems from the reaction site outwards (particularly for T.S. calcs).

## Modelling relative rates



## Modelling relative rates



relative to their own respective uncomplexed starting material


Pictures from MacMolPIt (also free)

## Modelling relative rates



HOMO of TS
Vector arrow of TS vibration


Pictures from MacMoIPIt (also free)

