

# Variation of selectivity coefficients: impact on column efficiency

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# Context of the study

- **Selectivity variations have been described experimentally:**  
=> Bonner, Argersinger, Helfferich, Soldatov, Högfeldt, Shallcross, Höll...
- **Some models have been proposed to take into account this phenomenon:**  
=> Three Parameter Model, Soldatov model, Wilson, Regular solid solution, Surface complexation, multisite sorption
- **Few attempts have been made to include selectivity variation in a reactive transport code**
- **Objective : to model a deep bed column of Ion Exchange Resin at equilibrium taking into account selectivity variation**

# 1

## 1. Theoretical background

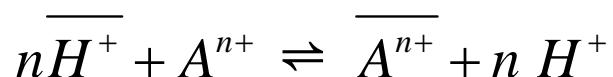
- Different formalisms
- Selectivity coefficient and thermodynamic constant
- Three Parameter Model

2. Equilibrium study : Ni and Cs selectivity

3. Modelling variable selectivity coefficient : impact on the ion retention

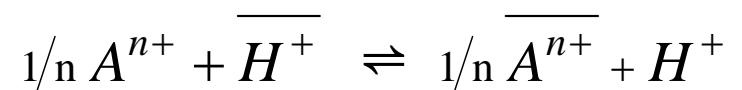
## Different formalisms

Gaines-Thomas convention



Resin / solution  
exchange reaction

Bonner study<sup>1</sup>: Vanselow convention



<sup>4</sup>  
<sup>1</sup> Bonner O.D., Smith L.L., 1957: "A selectivity scale for some divalent cations on Dowex 50", *The Journal of Physical Chemistry*, **61**, pp.326-329.

# Different formalisms

Gaines-Thomas convention

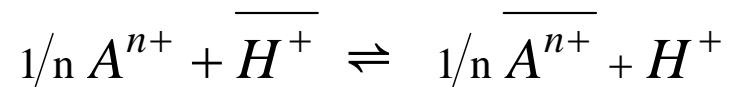


$$_H^K_{GT} = \frac{\overline{a_{A^{n+}}} \times (a_{H^+})^n}{(\overline{a_{H^+}})^n \times a_{A^{n+}}}$$

Resin / solution  
exchange reaction

Thermodynamic  
equilibrium constant

Bonner study<sup>1</sup>: Vanselow convention



$$_H^K_B = \frac{(\overline{a_A})^{1/n} \times a_H}{\overline{a_H} \times (\overline{a_A})^{1/n}}$$

# Different formalisms

Gaines-Thomas convention



$$_H^K_{GT} = \frac{\overline{a}_{A^{n+}} \times (\overline{a}_{H^+})^n}{(\overline{a}_{H^+})^n \times \overline{a}_{A^{n+}}}$$

$$\overline{a}_i = \overline{E}_i \times \gamma_i \quad \overline{E}_i = \frac{z_i \cdot \overline{C}_i}{EC}$$

Equivalent fraction

Resin / solution exchange reaction

Thermodynamic equilibrium constant

Activity of sorbed ions

Bonner study<sup>1</sup>: Vanselow convention



$$_H^K_B = \frac{(\overline{a}_A)^{1/n} \times a_H}{a_H \times (\overline{a}_A)^{1/n}}$$

$$\overline{a}_i = \overline{x}_i \times \gamma_i \quad \overline{x}_i = \frac{\overline{C}_i}{\sum_j \overline{C}_j \text{ counter-ions}}$$

Molar fraction

<sup>6</sup>  
<sup>1</sup> Bonner O.D., Smith L.L., 1957: "A selectivity scale for some divalent cations on Dowex 50", *The Journal of Physical Chemistry*, **61**, pp.326-329.

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Equivalent fraction

$$_H^K_{GT}^a = \frac{\overline{E}_{A^{n+}} \cdot (a_{H^+})^n}{\overline{E}_{H^+} \cdot a_{A^{n+}}}$$

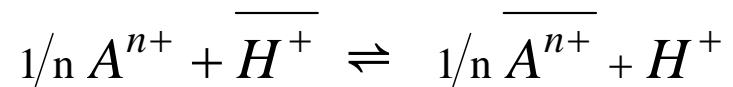
Resin / solution exchange reaction

Thermodynamic equilibrium constant

Activity of sorbed ions

Equivalent fraction

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$$_H^K_B = \frac{(\overline{a}_A)^{1/n} \times a_H}{a_H \times (\overline{a}_A)^{1/n}}$$

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Molar fraction

Corrected selectivity coefficient

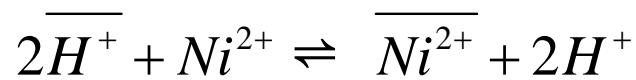
$$_H^K_B^a = \frac{(\overline{x}_A)^{1/n} \times (a_H)}{\overline{x}_H \times (a_A)^{1/n}}$$

<sup>7</sup>

<sup>1</sup> Bonner O.D., Smith L.L., 1957: "A selectivity scale for some divalent cations on Dowex 50", *The Journal of Physical Chemistry*, **61**, pp.326-329.

# Relation between selectivity coefficient and thermodynamic constant – H<sup>+</sup>/Ni<sup>2+</sup> exchange

Gaines-Thomas convention

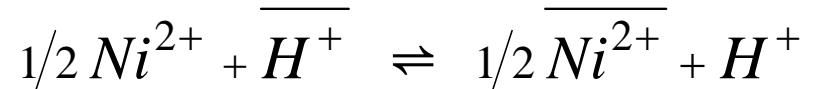


$$\frac{Ni}{H} K_{GT}^a = \frac{\overline{E_{Ni}} \cdot (a_H)^2}{\overline{E_H}^2 \cdot a_{Ni}}$$

Corrected selectivity coefficient

$$\frac{Ni}{H} K_{GT}^a = \left( \frac{Ni}{H} K_B^a \right)^2 \times 2 \left( 1 + \overline{x_{Ni}} \right)$$

Bonner study: Vanselow convention

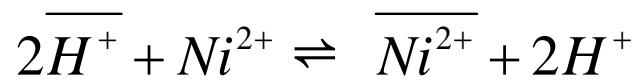


$$\frac{Ni}{H} K_B^a = \frac{\left( \overline{x_{Ni}} \right)^{1/2} \times (a_H)}{\overline{x_H} \times (a_{Ni})^{1/2}}$$

<sup>1</sup> Argersinger Jr. W.J., Bonner O.D., 1950: "Thermodynamics and Ion Exchange Phenomena", *Transactions of the Kansas Academy of Science* **53** (3): p. 404-410.

# Relation between selectivity coefficient and thermodynamic constant – H<sup>+</sup>/Ni<sup>2+</sup> exchange

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$$\frac{^{Ni}_H K_{GT}^a}{E_H^2 \cdot a_{Ni}} = \frac{\overline{E_{Ni}} \cdot (a_H)^2}{\overline{E_H}^2 \cdot a_{Ni}}$$

Corrected selectivity coefficient

$$\frac{^{Ni}_H K_{GT}^a}{E_H^2 \cdot a_{Ni}} = \left( \frac{^{Ni}_H K_B^a}{E_H} \right)^2 \times 2 \left( 1 + \overline{x_{Ni}} \right)$$



$$\ln \frac{^{Ni}_H K_{GT}}{E_H} = (z_H - z_{Ni}) + \int_0^1 \ln \frac{^{Ni}_H K_{GT}^a}{E_H} d\overline{E_{Ni}}$$

Thermodynamic equilibrium constant calculation<sup>1</sup>

$$\ln \frac{^{Ni}_H K_B}{E_H} = \int_0^1 \ln \frac{^{Ni}_H K_B^a}{E_H} d\overline{E_{Ni}}$$

$$\log \frac{^{Ni}_H K_{GT}}{E_H} = 2 \times \log \frac{^{Ni}_H K_B}{E_H}$$

<sup>1</sup> Argersinger Jr. W.J., Bonner O.D., 1950: "Thermodynamics and Ion Exchange Phenomena", *Transactions of the Kansas Academy of Science* **53** (3): p. 404-410.

# Coupling an equilibrium model with a reactive transport code : Three Parameter Model<sup>1</sup>

- Numerically easy to introduce in a reactive transport code
- The model should be adapted to CHESS<sup>2</sup> formalism
- Easy to linearize for numerical calculation techniques to be used
- Model that describes well the experimental data
  - Multisite approach: no good fit for a monovalent / divalent exchange
  - The Three Parameter Model (TPM) provides an easy-to-fit and an easy-to-use model : sorbed ion activities are incorporated in a lumped parameter

$$\log\left(\frac{^A}{^H}K_V^a\right) = \overline{x_A} \log\left(\frac{^A}{^H}K_V^a\left(\overline{x_A} \rightarrow 1\right)\right) + \left(1 - \overline{x_A}\right) \log\left(\frac{^A}{^H}K_V^a\left(\overline{x_A} \rightarrow 0\right)\right) + B\overline{x_A}\left(1 - \overline{x_A}\right)$$

<sup>1</sup> Högfeldt E., Soldatov V.S., 1979: "On the properties of solid and liquid ion exchangers – VII", *Journal of Inorganic and Nuclear Chemistry*, **41**, pp.575-577.

<sup>2</sup> Van der Lee J., 1998 : *Thermodynamic and mathematical concepts of CHESS*, Technical report LHM/RD/98/39, Ecole Nationale Supérieure des Mines de Paris, Centre de Géosciences, France.

# 2

1. Theoretical background

## 1. Equilibrium study : Ni and Cs selectivity

- Experimental protocol
- Imprecision analysis
- Selectivity variation plots

3. Modelling variable selectivity coefficient : impact on the ion retention

# Nickel chloride exchange: batch procedure

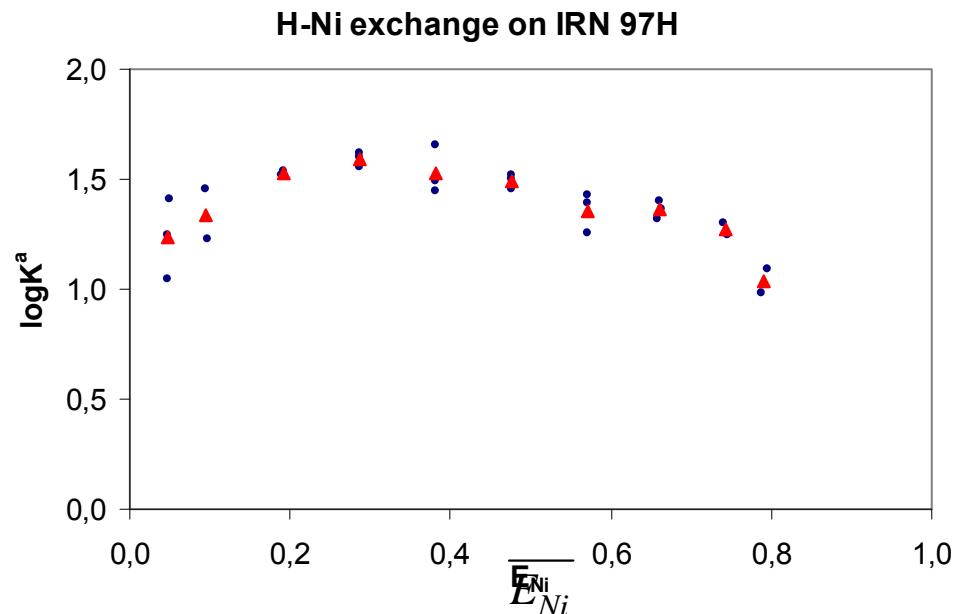
- **n mL of a mother solution at  $C_{\text{mother}} = 1400 \text{ ppm}_{\text{Ni}} \pm 3\%$  are mixed with UP water in a V = 50 mL gauged vial :  $C_0 = 70 \text{ to } 630 \text{ ppm}_{\text{Ni}}$**
- **m = 0.5 g<sub>humid</sub> ± 0.05g of IRN 97H (Rohm&Haas) are poured in the beaker**
- Stirring for 3 hours with a magnetic stirrer
- **pH (± 0.05) is measured at 25 °C**
- **$C_{\text{eq}} = \text{Ni}^{2+}$  equilibrium concentration measured by ICP-AES/MS (± 2- 10%)**
- **EC = Exchange capacity =  $2.5 \pm 0.15 \text{ meq/g}_{\text{humid}}$**



# Experimental uncertainties analysis

$$_{H^{Ni}}K_{GT}^a = \frac{\overline{E_{Ni}} \cdot (a_H)^2}{\overline{E_H}^2 \cdot a_{Ni}}$$

$$\overline{E_i} = \frac{z_i \cdot V \cdot \left( \overline{C_{mother}} / dilution - \overline{C_{eq}} \right)}{EC}$$

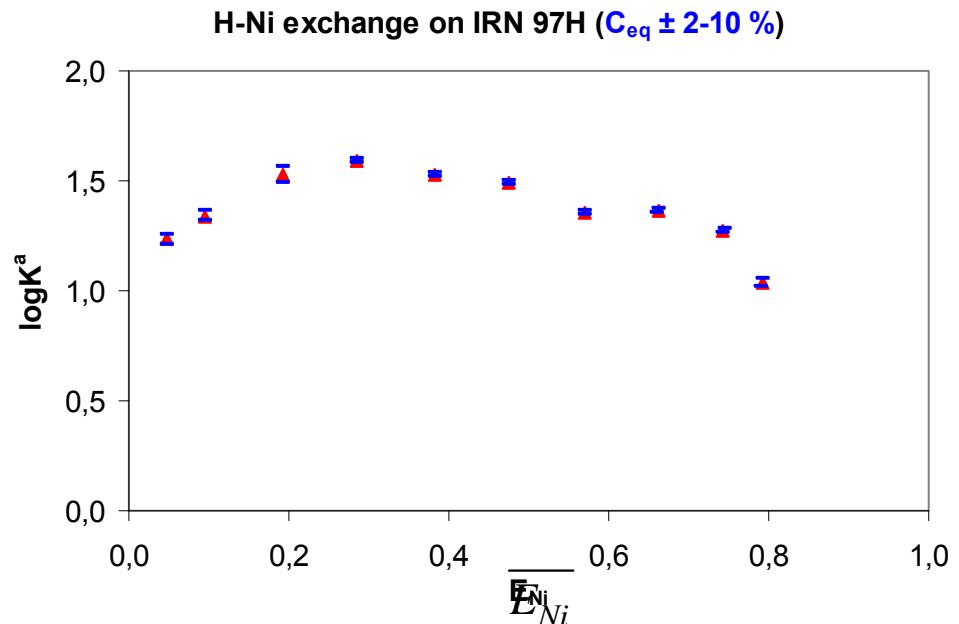


- Large variation of selectivity coefficient
- Saturation < 80% because of acidification

# Experimental uncertainties analysis

$$\frac{N_i}{H} K_{GT}^a = \frac{\overline{E_{Ni}} \cdot (a_H)^2}{\overline{E_H}^2 \cdot a_{Ni}}$$

$$\frac{E_i}{E} = \frac{z_i \cdot V \cdot \left( \overline{C_{mother}} / dilution - \overline{C_{eq}} \right)}{EC}$$

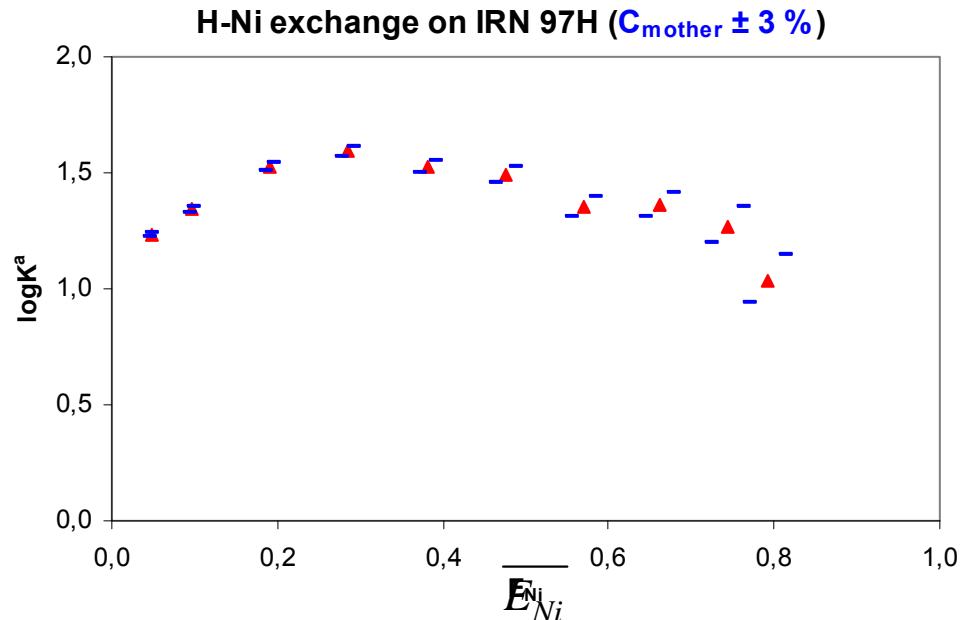


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- Experimental uncertainties: strong impact of pH, EC and  $C_{mother}$

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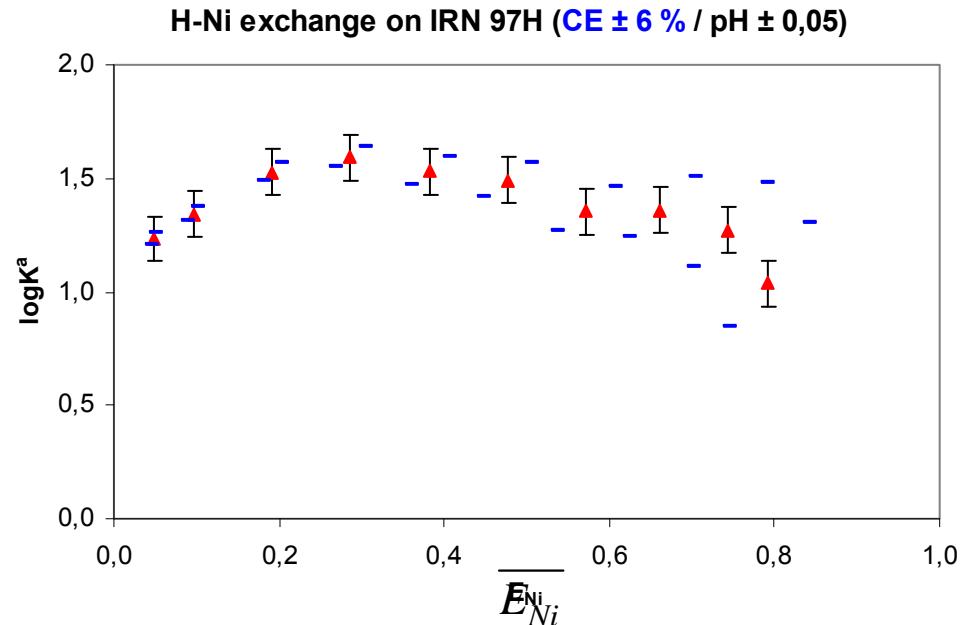


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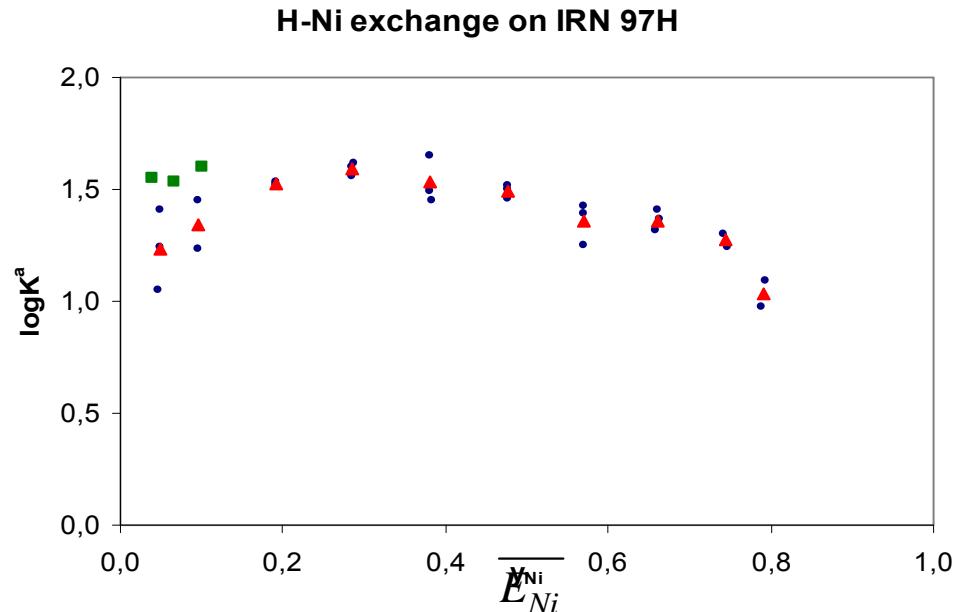


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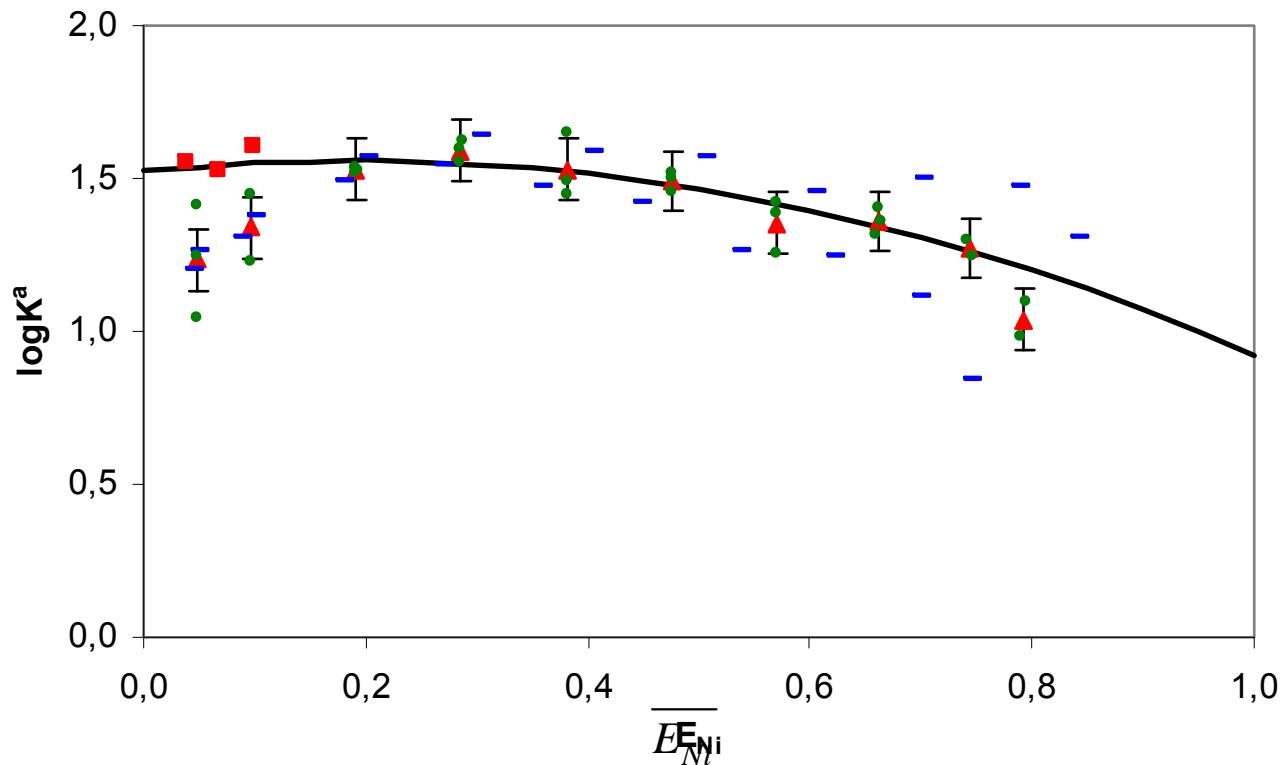
- Large variation of selectivity coefficient
- Saturation < 80% because of acidification
- Pollution problems for the 2 first points (fixed by acidification)
- Experimental uncertainties: strong impact of pH, EC and  $C_{mother}$

# Nickel selectivity coefficient variations

50 mL,  $[NiCl_2] = 70$  to  $630$  ppm<sub>Ni</sub>

IRN97H mass = 0.5 g<sub>humid</sub>

H-Ni exchange on IRN 97H (EC ± 6 % / pH ± 0,05)

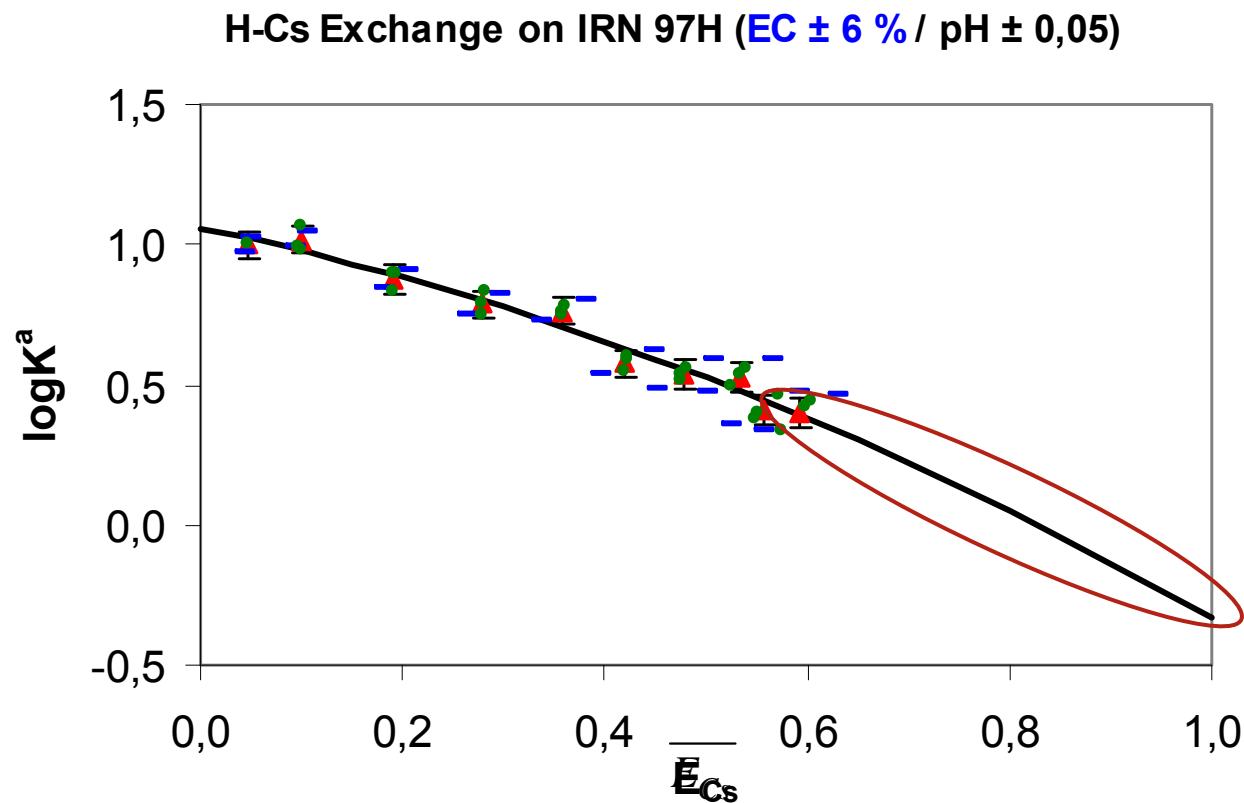


$\log_H^A K_{GT}^a (\overline{E}_A \rightarrow 0)$	1.52
$\log_H^A K_{GT}^a (\overline{E}_A \rightarrow 1)$	0.92
$B$	0.96
$\log_H^A K_{GT}$ 10,5% DVB	0.95
$\log_H^A K_{GT,Bonner}$ 8% DVB	1.19
$\log_H^A K_{GT,Bonner}$ 16% DVB	1.22

# Cesium selectivity coefficient variations

50 mL, [CsCl] = 160 to 2900 ppm<sub>Cs</sub>

IRN97H mass = 0.5 g<sub>humid</sub>



Importance of extrapolation

# 3

1. Theoretical background
2. Equilibrium study : Ni and Cs selectivity

## **1. Modelling variable selectivity coefficient : impact on the ion retention**

- Model developments
- Impact of selectivity variations on the retention in a deep bed experiment

# Model developments

- Based on modified TPM (Gaines-Thomas formalism)

$$\log\left({}^A_H K_{GT}^a\right) = \overline{E}_A \log\left({}^A_H K_{GT}^a \left(\overline{E}_A \rightarrow 1\right)\right) + \left(1 - \overline{E}_A\right) \log\left({}^A_H K_{GT}^a \left(\overline{E}_A \rightarrow 0\right)\right) + B_{GT} \overline{E}_A \left(1 - \overline{E}_A\right)$$

- Correction factor  $\overline{\gamma}$  to account for non idealities in the resin phase incorporated in the chemical speciation code CHESS

$$\log \overline{\gamma} = \left( \log {}^A_H K_{GT}^a - a \right) - b \overline{E}_A - c \overline{E}_A^2$$

$$a = \log {}^A_H K_{GT}^a \left( \overline{E}_A \rightarrow 0 \right); b = B_{GT} - \log {}^A_H K_{GT}^a \left( \overline{E}_A \rightarrow 0 \right) + \log {}^A_H K_{GT}^a \left( \overline{E}_A \rightarrow 1 \right); c = -B_{GT}$$

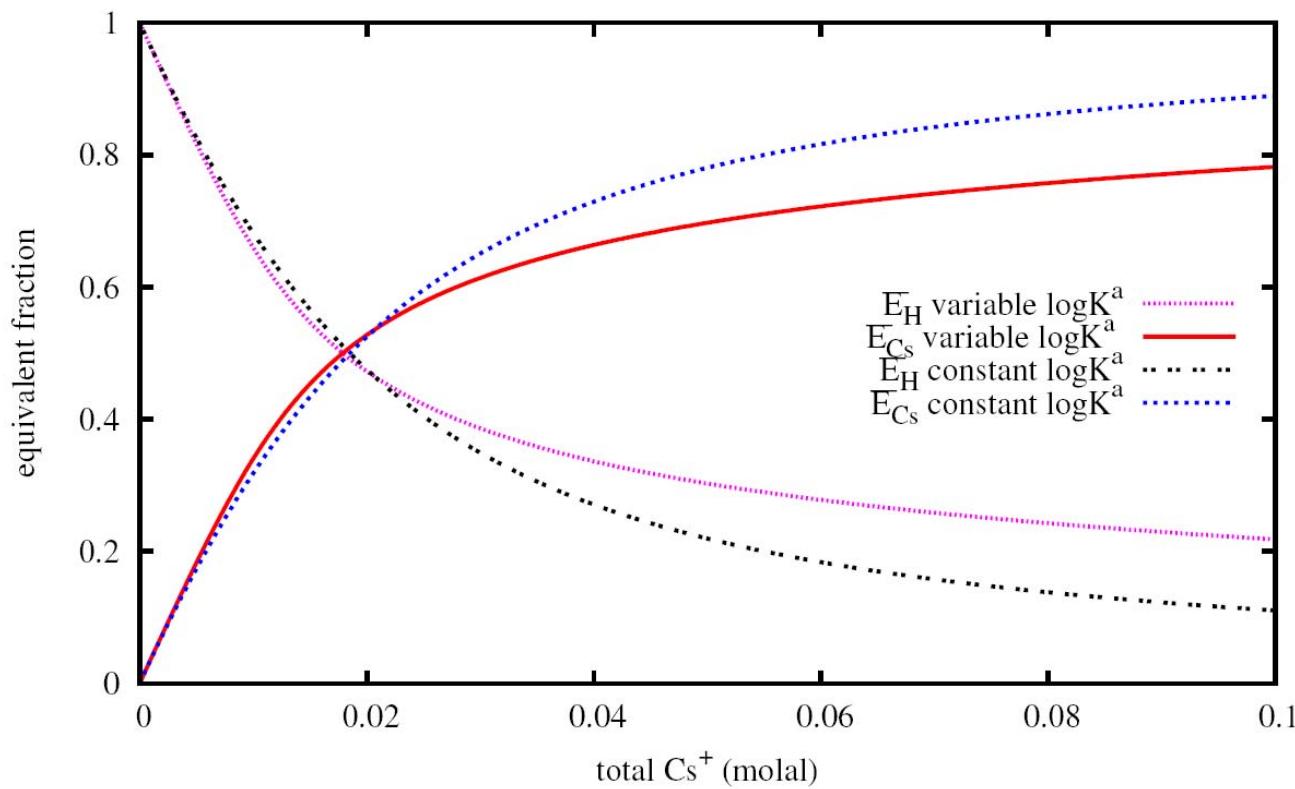
- Linearization of the mass action law to calculate equivalent fractions

$$\log \overline{E}_A = \log {}^A_H K_{GT}^a - \log \overline{\gamma} - n \log a_H + n \log \overline{E}_H + \log a_A$$

# Impact of $\log K^a$ variation on batch sorption

- **Simulations of a batch saturation experiment :**

- 0.5 g<sub>humid</sub> in 50 mL
- Initial concentration of Cs<sup>+</sup> ranging from 0 to 0.1 mol/L



➤ **Significant impact of selectivity variations on site occupancy**

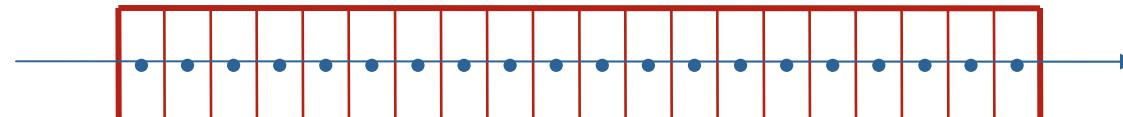


# Reactive transport coupling code at equilibrium

- Including the model to the reactive transport code HYTEC<sup>1</sup>
- This allows to simulate a column experiment.
- HYTEC solves the transport equation while calculating equilibrium chemistry in each node for each step, by finite volumes.
- Assumption of an homogeneous flow through the deep bed (1D calculation).
- Equilibrium model: we have not considered any kinetics in the system.

$$\omega \frac{\partial C_i}{\partial t} + \omega \frac{\partial \bar{C}_i}{\partial t} = -u \frac{\partial C_i}{\partial x} \quad \omega = \text{porosity}$$

$$\bar{C}_i = \text{CHESS}(C_i, C_j \dots) \quad u = \text{filter velocity (m/s)}$$



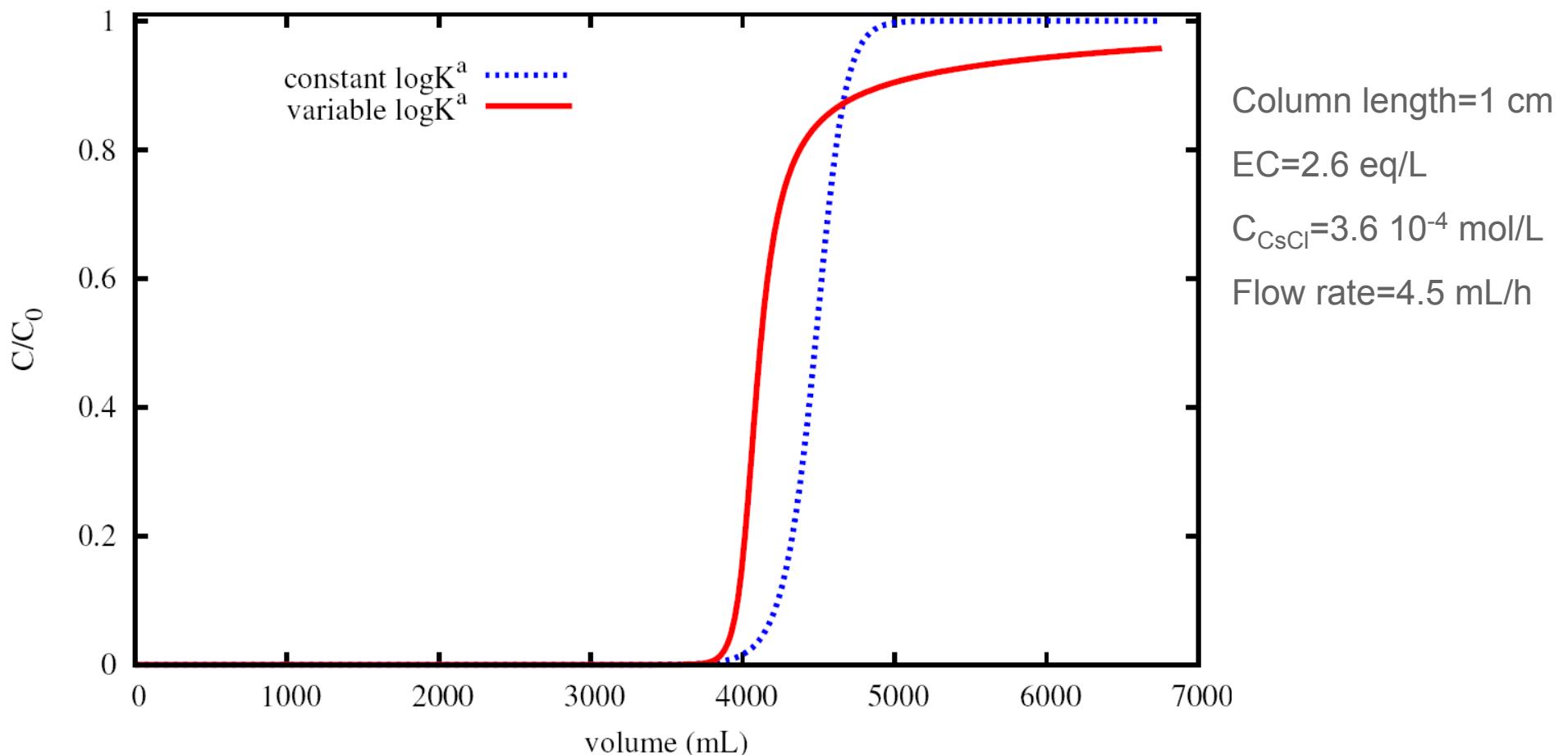
<sup>1</sup> Van der Lee J. et al, 2003 : "Module-oriented modeling of reactive transport with HYTEC", *Computers & Geosciences*, 29(3) pp. 265-275.

# Impact of $\log K^a$ variation of cesium on sorption (film)

- **Test case:**

- Column length = 1 cm
- $EC_{IRN\ 97H} = 2.6\ eq/L$
- $C_{CsCl} = 3.6\ 10^{-4}\ mol/L$
- Flow rate = 4.5 mL/h

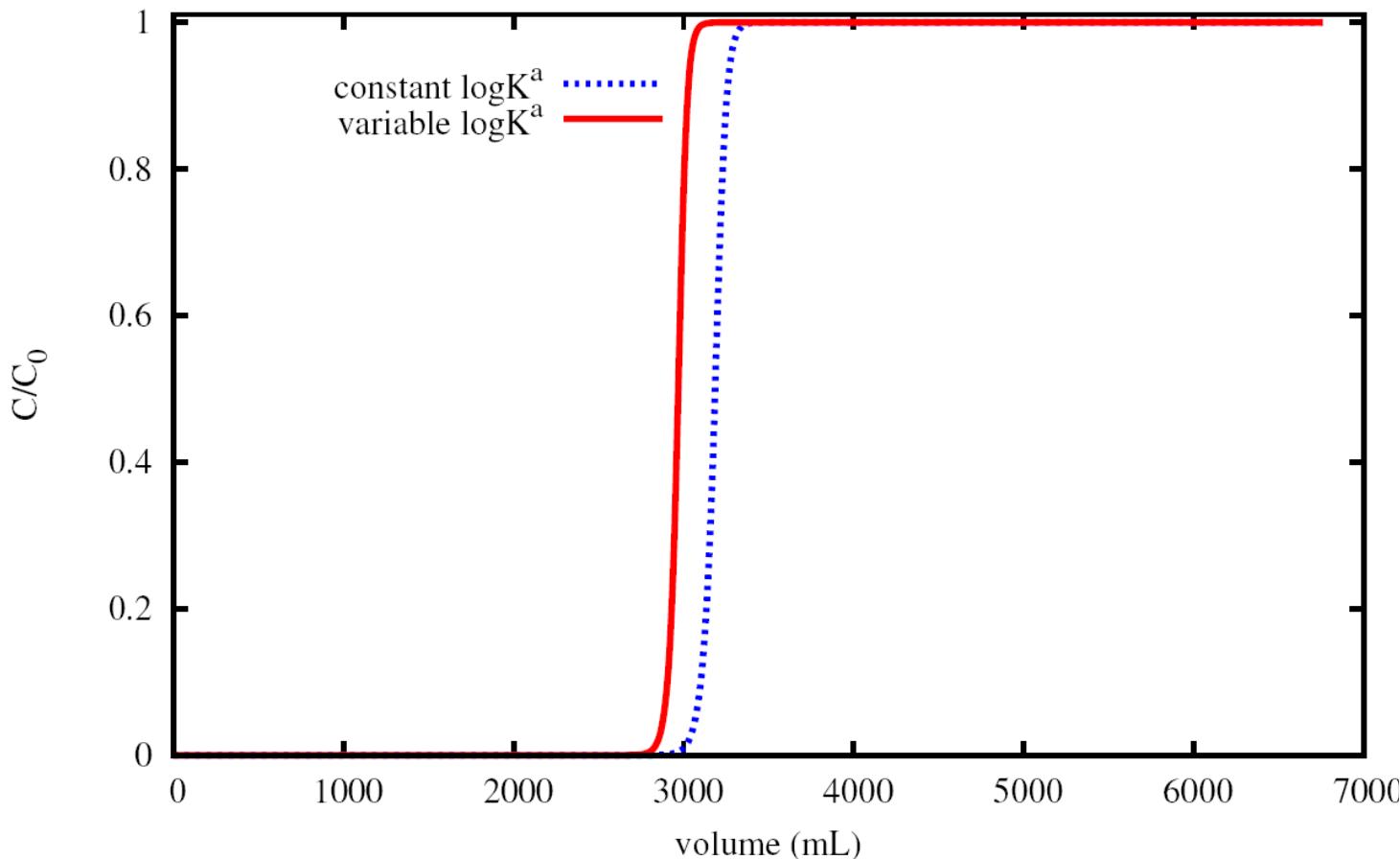
# Impact of $\log K^a$ variation of cesium on sorption (breakthrough curve)



25

- Significant impact on cesium retention
- Compressive front turns dispersive

# Impact of $\log K^a$ variation of nickel on sorption (breakthrough curve)



Column length=1 cm  
EC=2.6 eq/L  
 $C_{\text{NiCl}_2}=1.8 \cdot 10^{-4} \text{ mol/L}$   
 $=3.6 \cdot 10^{-4} \text{ eq/L}$   
Flow rate=4.5 mL/h  
 $C_{\text{HCl}}=10^{-2} \text{ mol/L}$

- Nickel leaches earlier when  $K^a$  varies
- Electroselectivity: nickel is well retained
- Potential impact on nickel retention

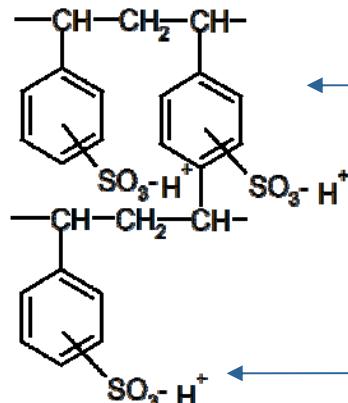
## Conclusions

- Selectivity coefficients can vary of 1 order of magnitude.
  - We propose a model for divalent/monovalent exchange with non-ideality correction.
  - We applied a reactive transport code to simulate ion retention in deep bed columns at equilibrium.
- We showed that selectivity variations should be accounted for when modelling ion exchange resins.

## WHAT'S NEXT ?

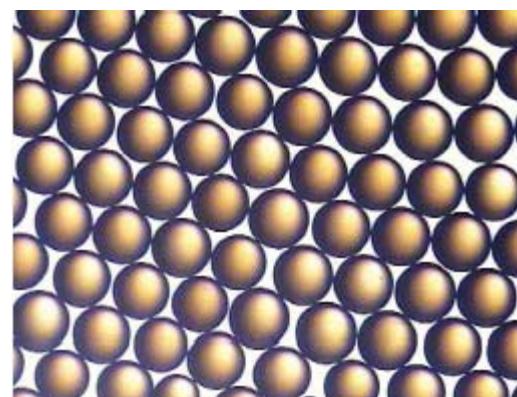
- To compare model with experimental results
  - We should refine the non-ideality model: regular solid solutions are considered.
  - This model will be better suited to deal with multicomponent exchange.
- <sup>27</sup> • We will incorporate kinetics and impact of flow rate in HYTEC.

# Structure of the resin studied : IRN 97H (Rohm&Haas)



polystyrene skeleton cross-linked with  
DiVinylBenzene

Functional groups:  
Sulfonic acids for a strong acidic cation exchanger



Gel type

	Water retention	Crosslinkage	Ion exchange capacity	Beads diameter
R&H	45 – 49 %	10 %	2.25 eq/L <sub>H</sub>	525 ± 25 µm
Exp	53 %	/	2.16 eq/L <sub>H</sub> – 2.6 meq/g	/

# Regular solid solutions



## Calculation of activity coefficients inside the resin phase

Binary exchange

$$RT \ln \overline{\gamma_1} = W_{12}^G \left(1 - \overline{x_1}\right)^2$$

Multicomponent exchange

$$RT \ln \overline{\gamma_1} = \sum_{j>1}^n W_{1j}^G \overline{x_j} \left(1 - \overline{x_1}\right) - \sum_{i>1}^n \sum_{j>i}^n W_{ij}^G \overline{x_i} \overline{x_j} + \sum_{i>1}^n \sum_{j>i}^n W_{1ij}^G \overline{x_i} \overline{x_j} \left(1 - 2 \cdot \overline{x_1}\right) - \sum_{i>1}^n \sum_{j>i}^n \sum_{k>j}^n W_{ijk}^G \overline{x_i} \overline{x_j} \overline{x_k}$$

- Large knowledge in soil science (mineralogy)
- Model developed for solid solution where exchange are largely homovalent

# WILSON model

- ✓ Calculation of activity coefficients inside the resin phase

$$\ln \bar{\gamma}_i = 1 - \ln \left( \sum_{j=1}^m \bar{x}_j \lambda_{ij} \right) - \sum_{k=1}^m \frac{\bar{x}_k \lambda_{ki}}{\sum_{j=1}^m \bar{x}_j \lambda_{kj}}$$

- Independent of experimental conditions
- Many binary interaction parameters  $\lambda_{ij}$  not widely known

## SOLDATOV model

- ✓ **Explicit variation of the selectivity coefficient according to a polynomial which degree is a function of cross-linking**

$$K = cste$$

$$K = y(0,0)(1 - \bar{x}) + y(0,1)\bar{x}$$

$$K = y(2,0)(1 - \bar{x})^2 + 2y(1,1)(1 - \bar{x})\bar{x} + y(0,2)\bar{x}^2$$

$$K = y(3,0)(1 - \bar{x})^3 + 3y(2,1)(1 - \bar{x})^2\bar{x} + 3y(1,2)(1 - \bar{x})\bar{x}^2 + y(0,3)\bar{x}^3$$

$$K = y(4,0)(1 - \bar{x})^4 + 4y(3,1)(1 - \bar{x})^3\bar{x} + 6y(2,2)(1 - \bar{x})^2\bar{x}^2 + 4y(1,3)(1 - \bar{x})\bar{x}^3 + y(0,4)\bar{x}^4$$

- **Parameters are determined from the resin geometry, not function of experimental conditions**
- **Not developed for 2:1 exchange**
- **Extrapolation to multicomponent exchange**

## MELIS model

- ✓ **Surface complexation model (Nernst) + distribution of exchange sites (each site has its own sorption constant)**

$$K = (K_1)^{p_1} (K_2)^{p_2}$$

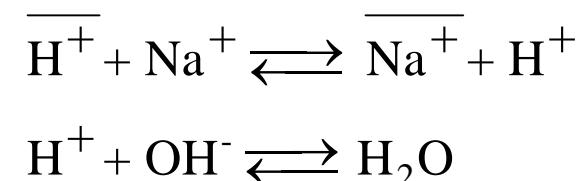
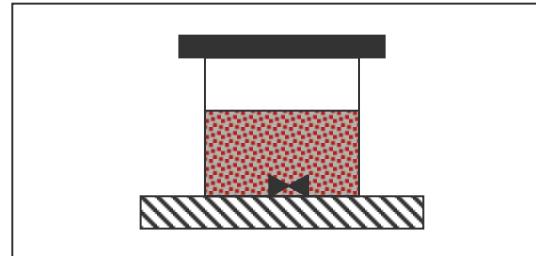
$$\gamma = \exp\left(-\frac{\sigma}{RT}\right) = \left(\frac{K_1}{K_2}\right)^{(p_1 p_2)^{1/2}}$$

$$K_j = \frac{\overline{y_{A^{n+},j}} \times \left(x_{H^+}\right)^n}{\left(\overline{y_{H^+,j}}\right)^n \times x_{A^{n+}}} \left(\frac{q_{0j}}{N}\right)^{1-n}$$

- **Surface complexation model can always be applied (even if it is far away from reality)**
- **Not adapted to 2:1 exchange**
- **Extrapolation to multicomponent exchange**

# Ion exchange capacity determination (EC)

- ✓ 0.5 g of regenerated resin
- ✓ 100 mL of 0.025M NaOH
- ✓ 2 hours stirring
- ✓ 50 mL are titrated for remaining OH<sup>-</sup>



	Exchange capacity (eq/g)	Exchange capacity (eq/L)
Experimental	$2.6 \pm 0.15 \text{ meq/g}$	$2.16 \pm 0.1 \text{ eq/L}$
Supplier, minimum	\	$2.00 \text{ eq/L}$
Supplier, found	\	$2.25 \text{ eq/L}$

- ✓ Differences originate from
  - ✓ Contact time (15 min vs 2 hours)
  - ✓ Sorption on HCl during regeneration
  - ✓ Sorption of NaOH during exchange

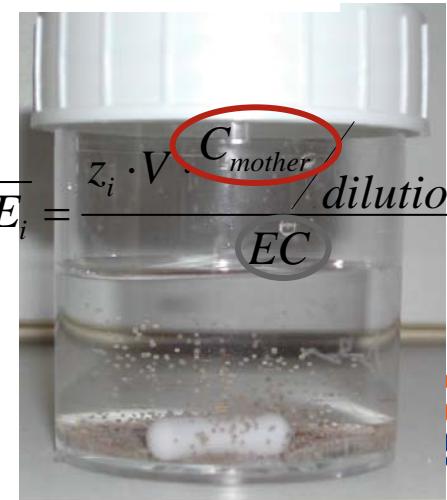
# Nickel chloride exchange: batch procedure

- **n mL of a mother solution at  $C_{mother} = 1400 \text{ ppm}_{Ni} \pm 3\%$**  are mixed with UP water in a  $V = 50 \text{ mL}$  gauged vial :  $C_0 = 70 \text{ to } 630 \text{ ppm}_{Ni}$
- **$m = 0.5 \text{ g}_{humid} \pm 0.05 \text{ g}$  of IRN 97H (Rohm&Haas)** are poured in the beaker
- Stirring for 3 hours with a magnetic stirrer
- **pH ( $\pm 0.05$ ) is measured at 25 °C**
- **$C_{eq} = \text{Ni}^{2+}$  equilibrium concentration measured by ICP-AES/MS ( $\pm 2\text{-}10\%$ )**
- **EC = Exchange capacity =  $2.5 \pm 0.15 \text{ meq/g}_{humid}$**
- **Hypothesis : Equilibrium concentration ( $C_{eq}$ ) << initial concentration ( $C_0$ )**

$$\log \frac{^{Ni}_H K_{GT}^a}{2} = \log \left( 2 \cdot V \cdot \frac{C_{mother}}{\text{dilution}} \right) + \log (EC) + \log (m) - 2pH$$

$$-2 \log \left( EC \cdot m - 2 \cdot V \cdot \frac{C_{mother}}{\text{dilution}} \right) - \log (C_{eq})$$

$$- \left\{ \frac{-0.5114 \times 4 \sqrt{2 \cdot \frac{C_{mother}}{\text{dilution}}} + 0.041 \times 2 \cdot \frac{C_{mother}}{\text{dilution}}}{1 + 0.3288 \times 3 \sqrt{2 \cdot \frac{C_{mother}}{\text{dilution}}}} \right\}$$



$$\overline{E_i} = \frac{z_i \cdot V \cdot \frac{C_{mother}}{\text{dilution}}}{EC}$$

<sup>34</sup> NB : For the ionic strength calculation, pH = H<sup>+</sup> concentration